

# Evaluating Security Against Rational Attackers

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# Papers covered

- Ahto Buldas, Peeter Laud, Jaan Priisalu, Märt Saarepera, Jan Willemson, *Rational Choice of Security Measures via Multi-Parameter Attack Trees*, in CRITIS 2006, LNCS 4347, pp. 235–248
- Aivo Jürgenson, Jan Willemson, *Processing Multi-parameter Attacktrees with Estimated Parameter Values*, in IWSEC 2007, LNCS 4752, pp. 308–319

# Motivation

- It is a complicated task to evaluate whether (IT-)infrastructure of a company is protected
  - sufficiently (i.e. achieving a satisfactory level), and
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- Even if the losses associated with vulnerability exploits can be estimated, the corresponding probabilities are very difficult to evaluate
- This is especially true for targeted, company-specific attacks, since the required statistics does not exist or is difficult to get

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# Rational Attackers and Attack Trees

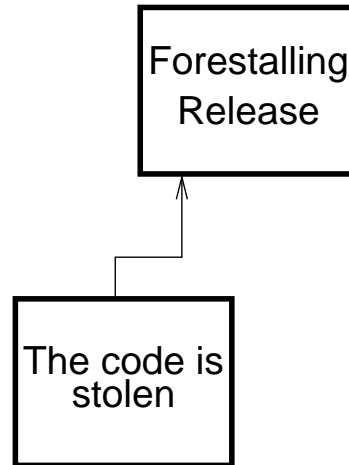
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- Such attacks can be modeled using gradual refinement starting from primary threats and breaking them down to elementary attacks
- As a result, we obtain an *attack tree*

# An Attack Tree

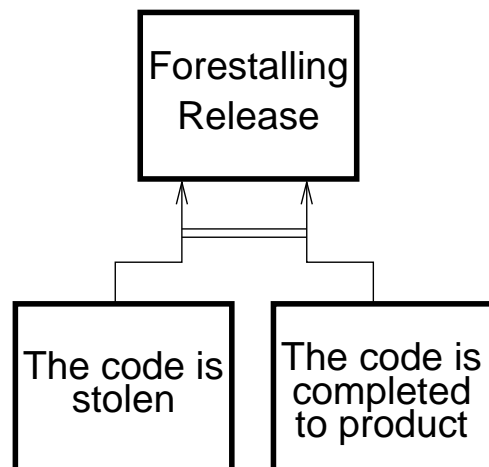


Forestalling  
Release

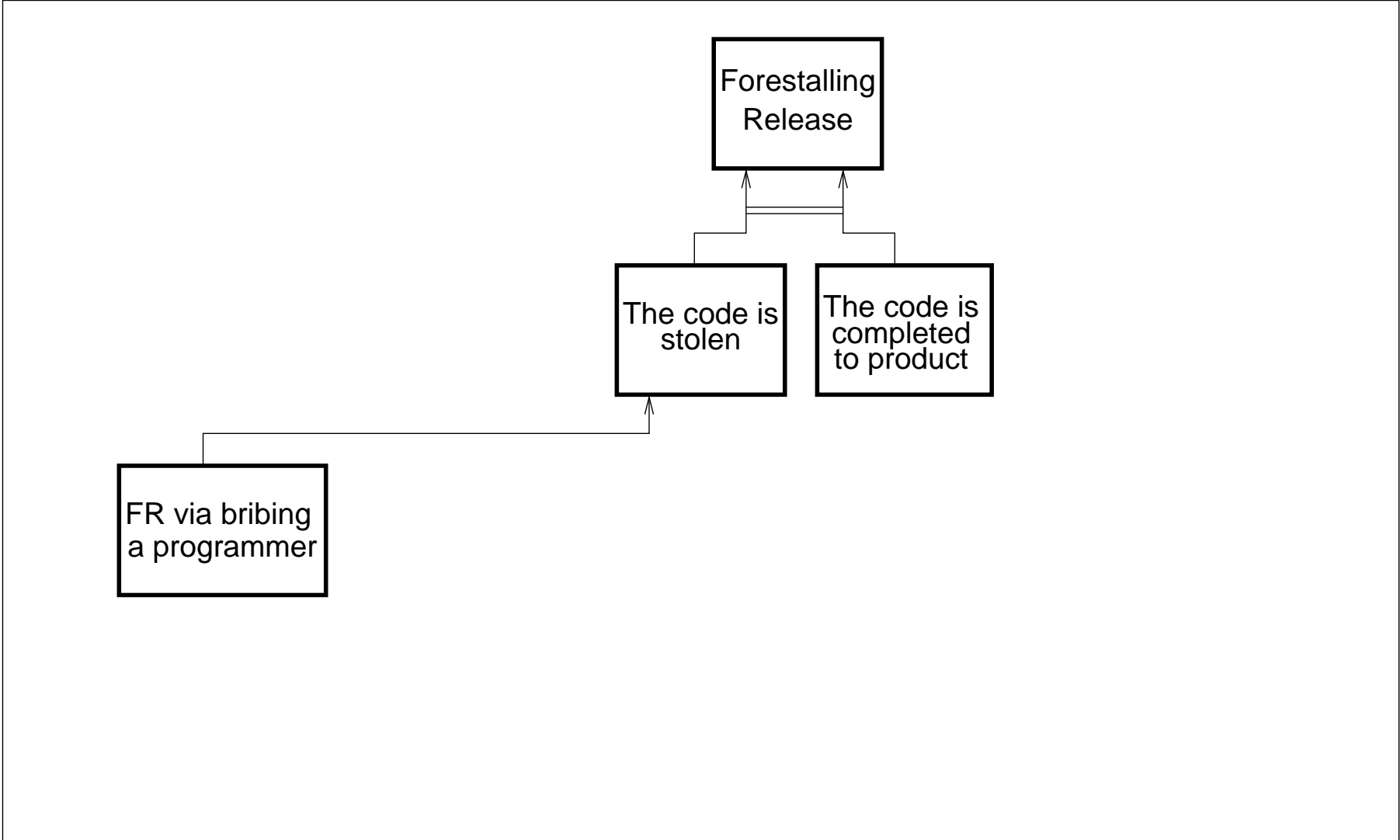
# An Attack Tree



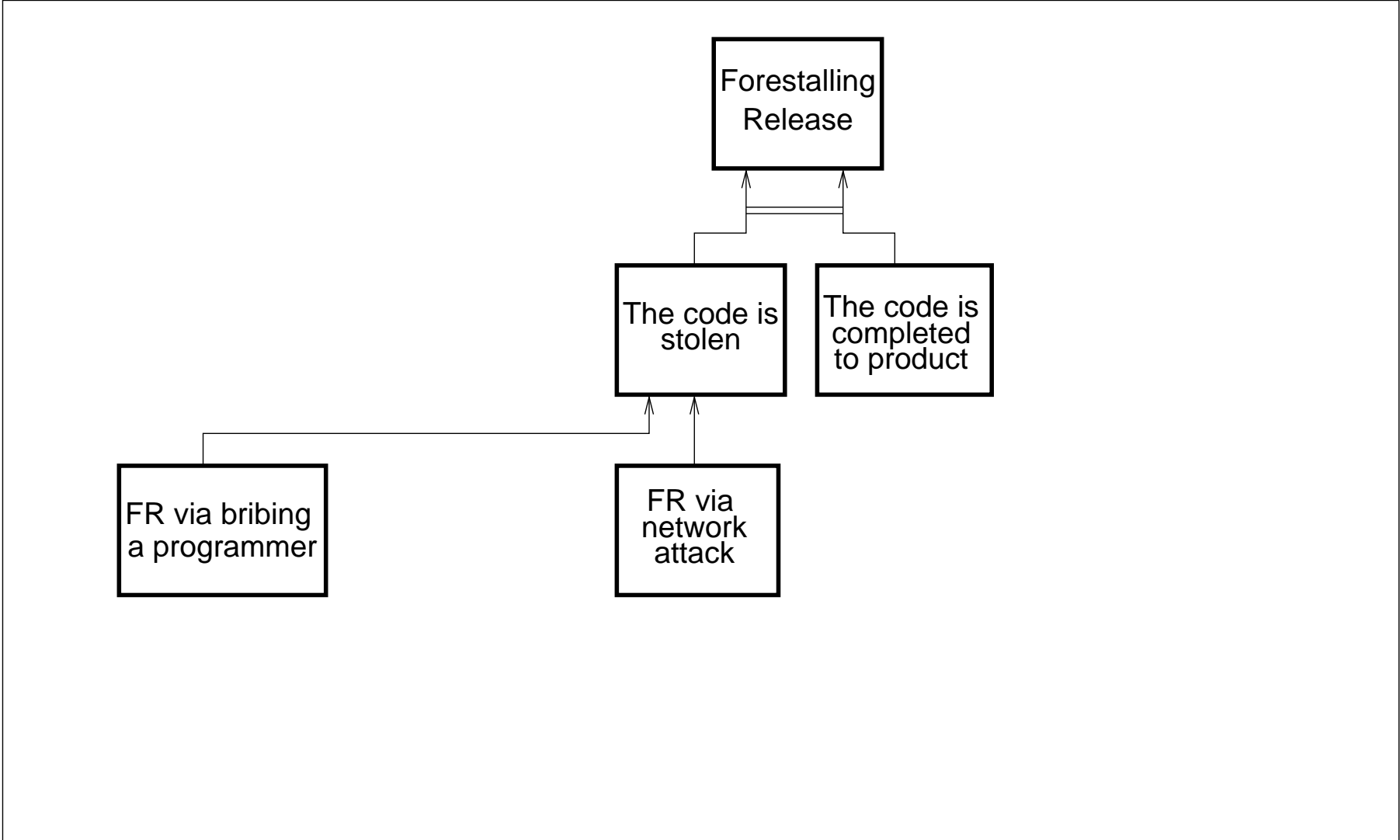
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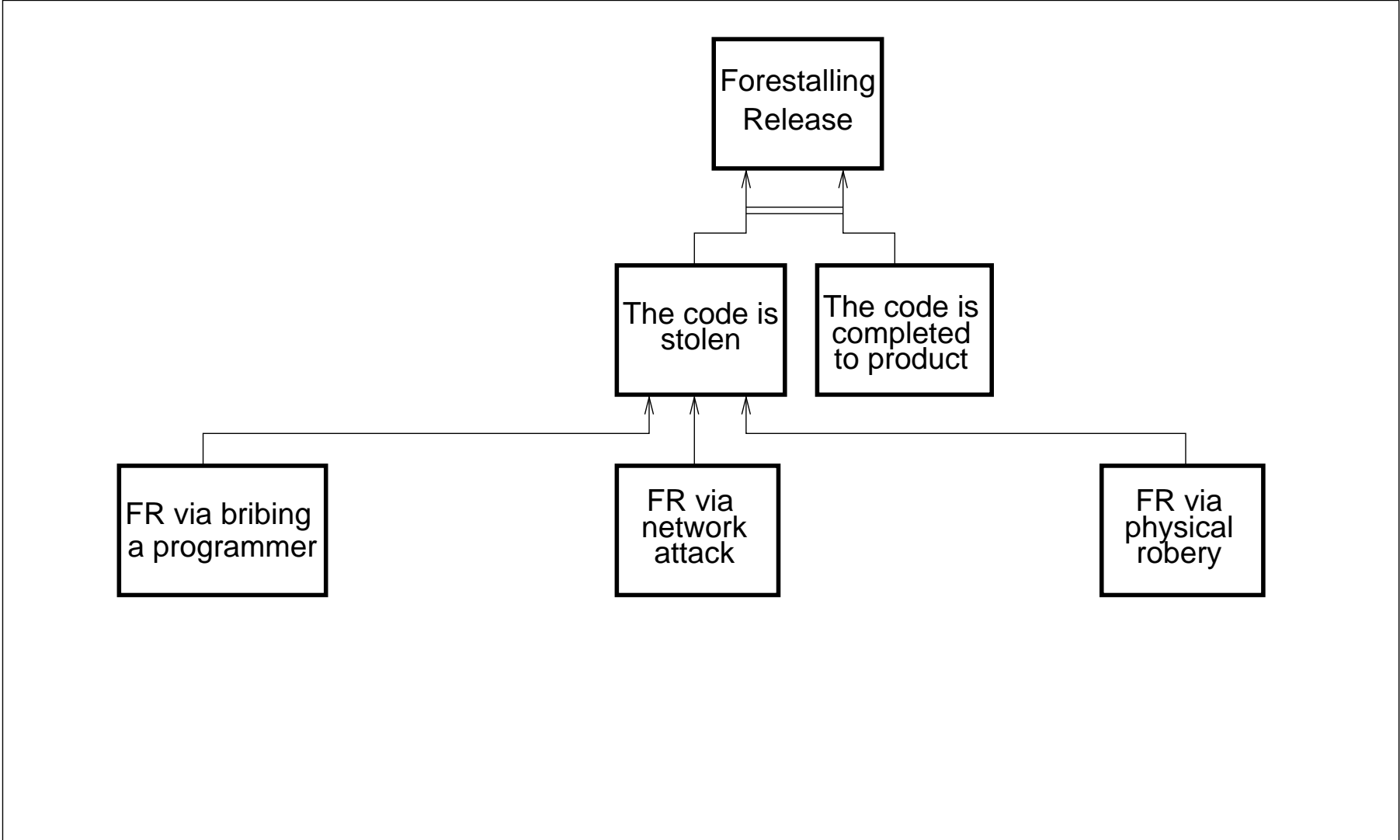
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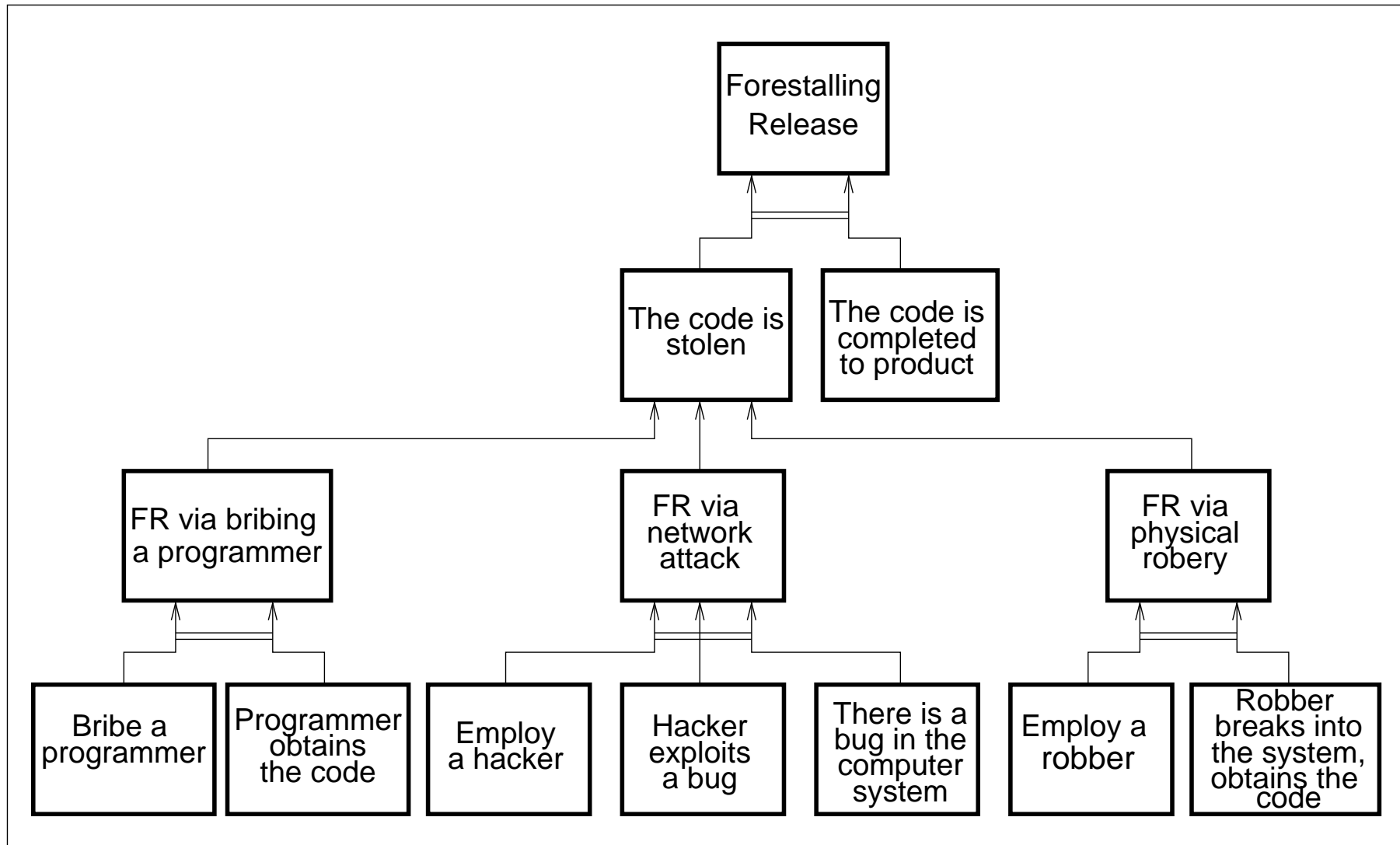
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# Parametrizing the Attack Tree

- When modelling the attack, we need to
  - set some parameter values to the leaves of the tree
  - define computation rules for parameter propagation

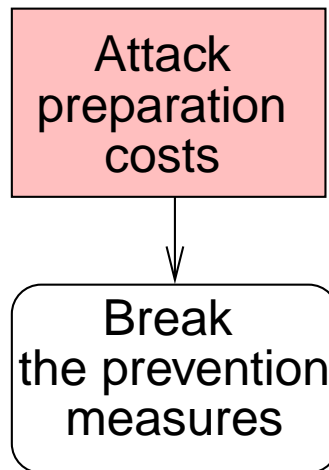
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- When modelling the attack, we need to
  - set some parameter values to the leaves of the tree
  - define computation rules for parameter propagation
- In this framework we will consider the following parameters:
  - Gains – the gains of the attacker if attack succeeds
  - Costs – the cost of the attack
  - $p$  – the success probability of the attack
  - $q$ , Penalties – the probability of getting caught and penalties (if the attack was successful)
  - $q_-$ , Penalties<sub>-</sub> – the probability of getting caught and penalties (if the attack was unsuccessful)

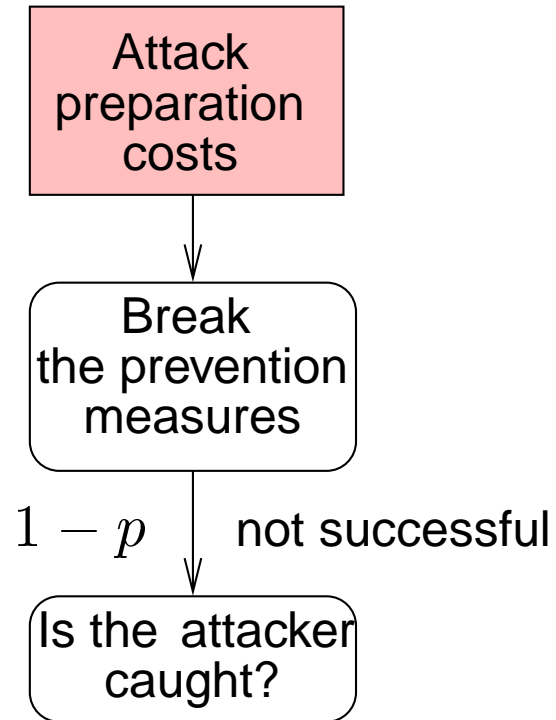
# The Attack Game

Attack  
preparation  
costs

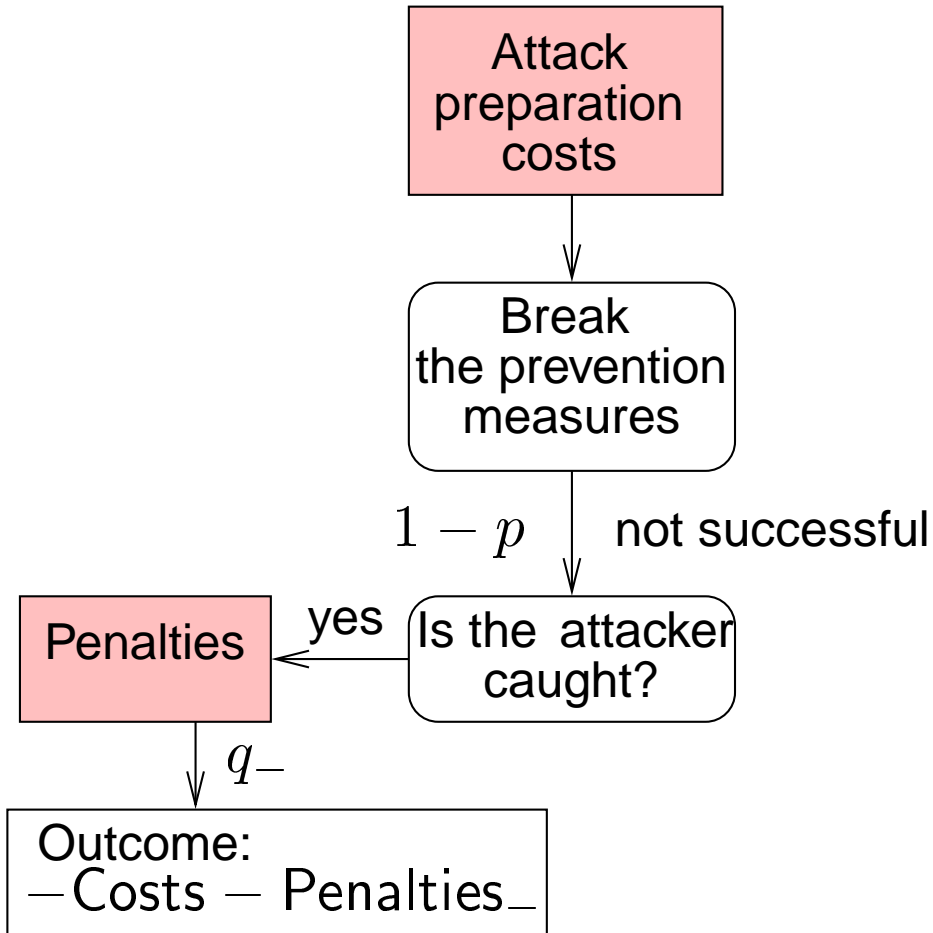
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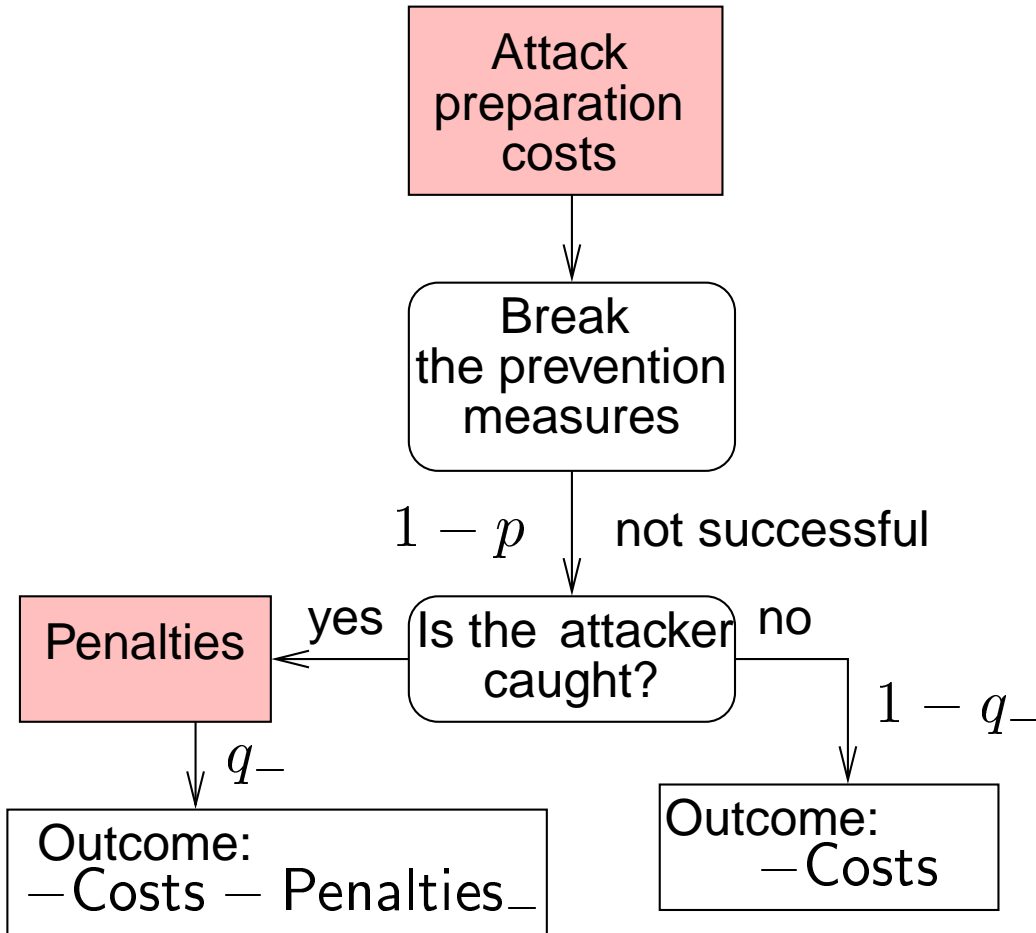
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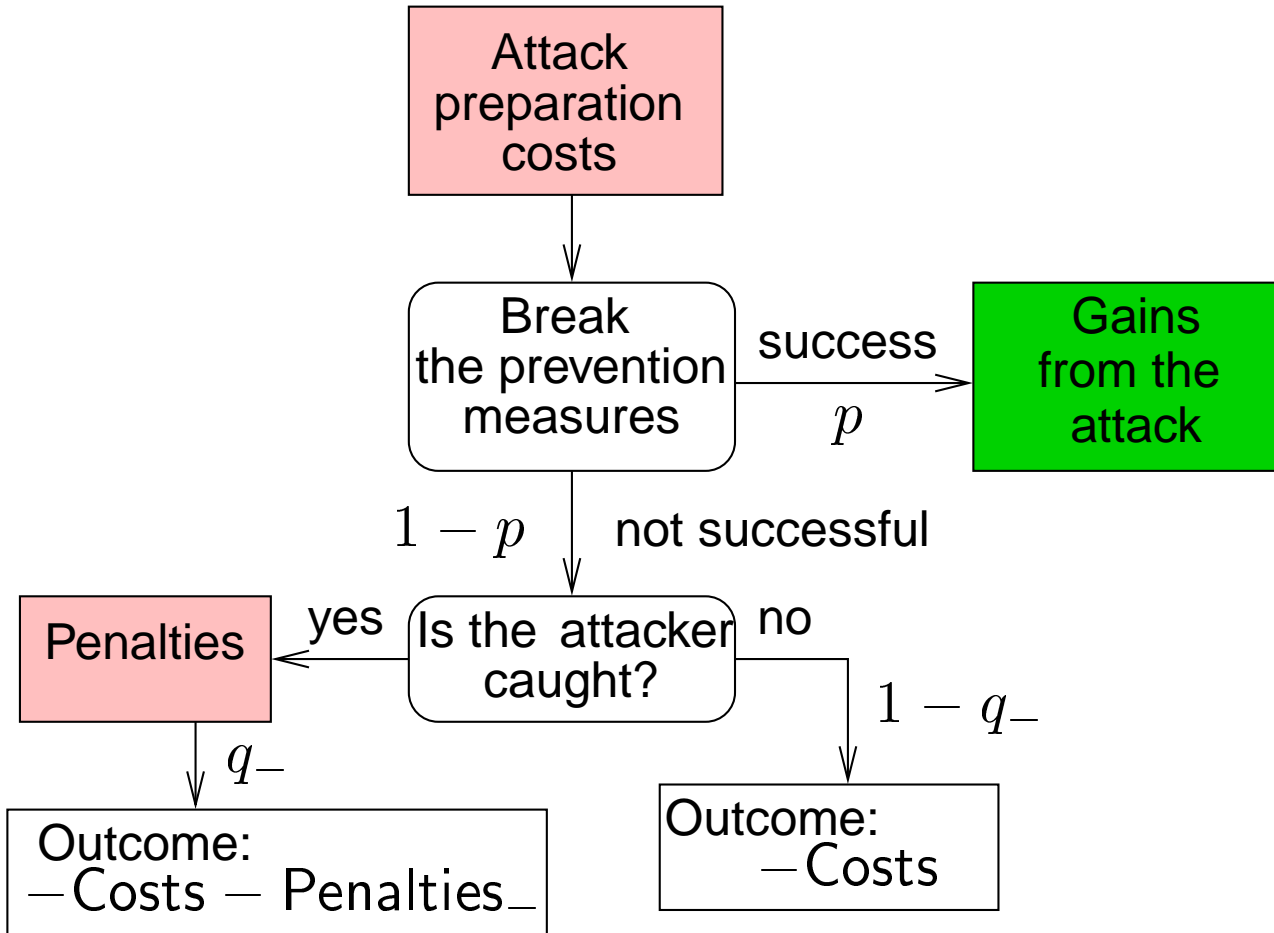
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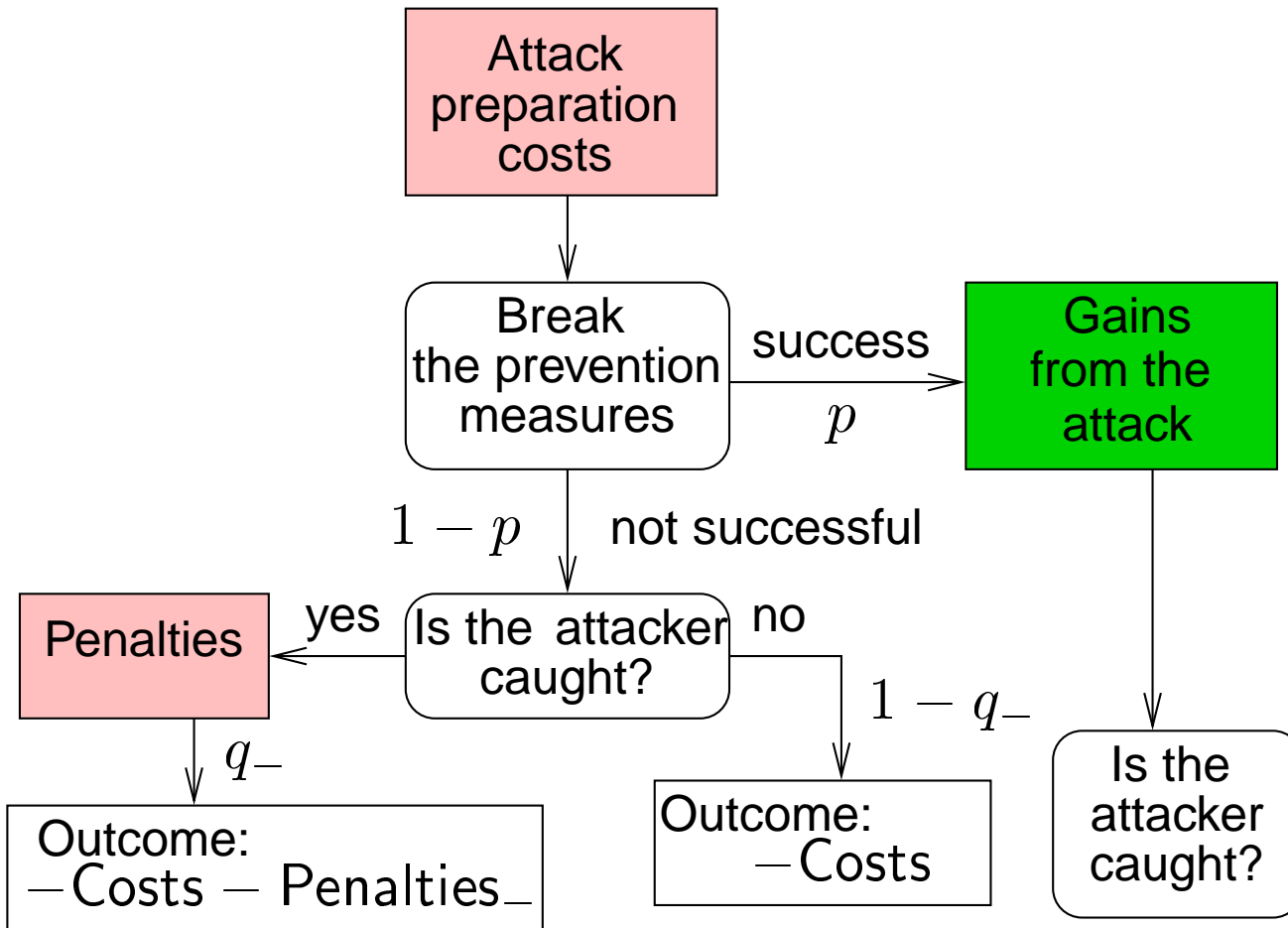


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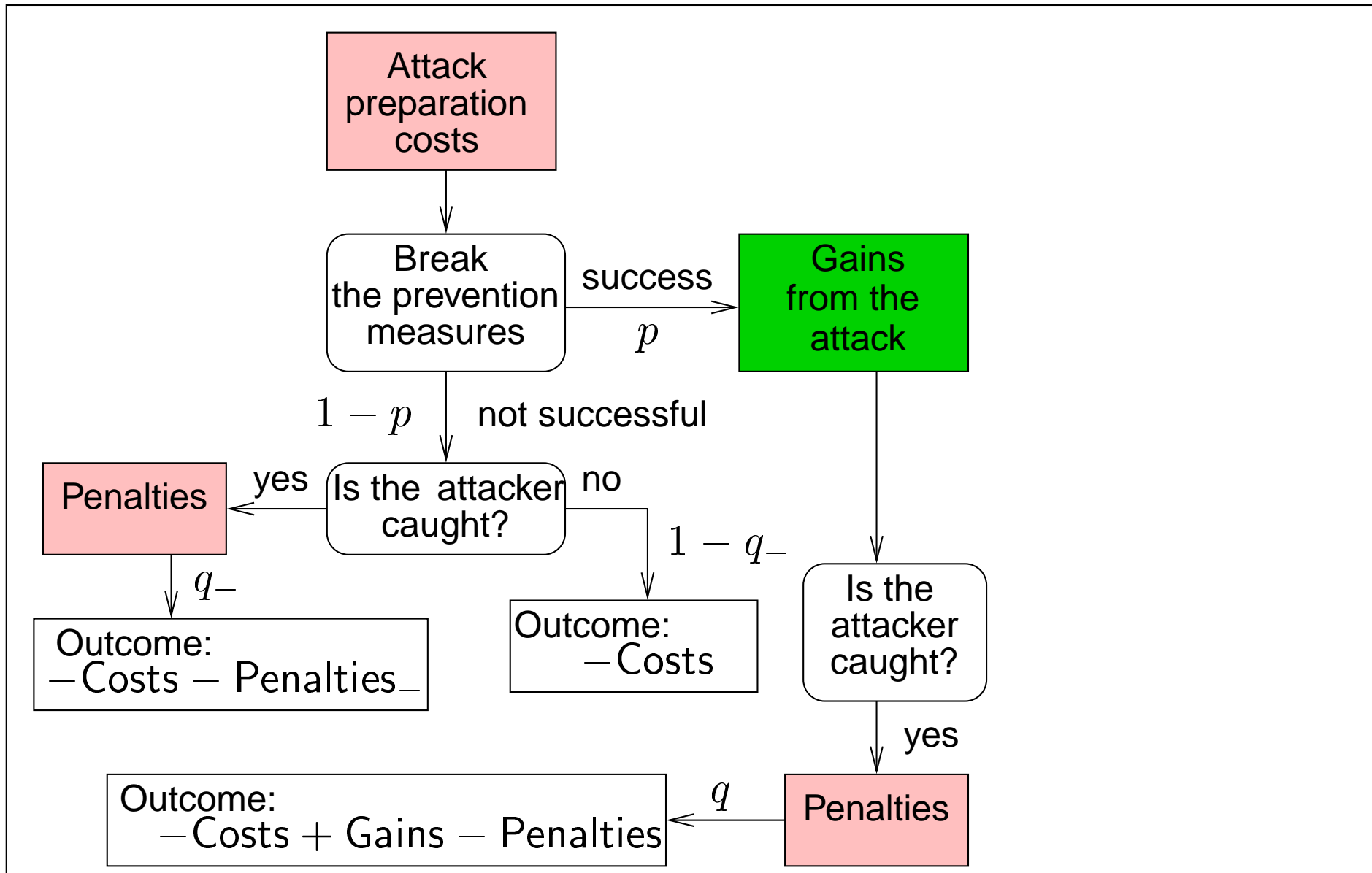




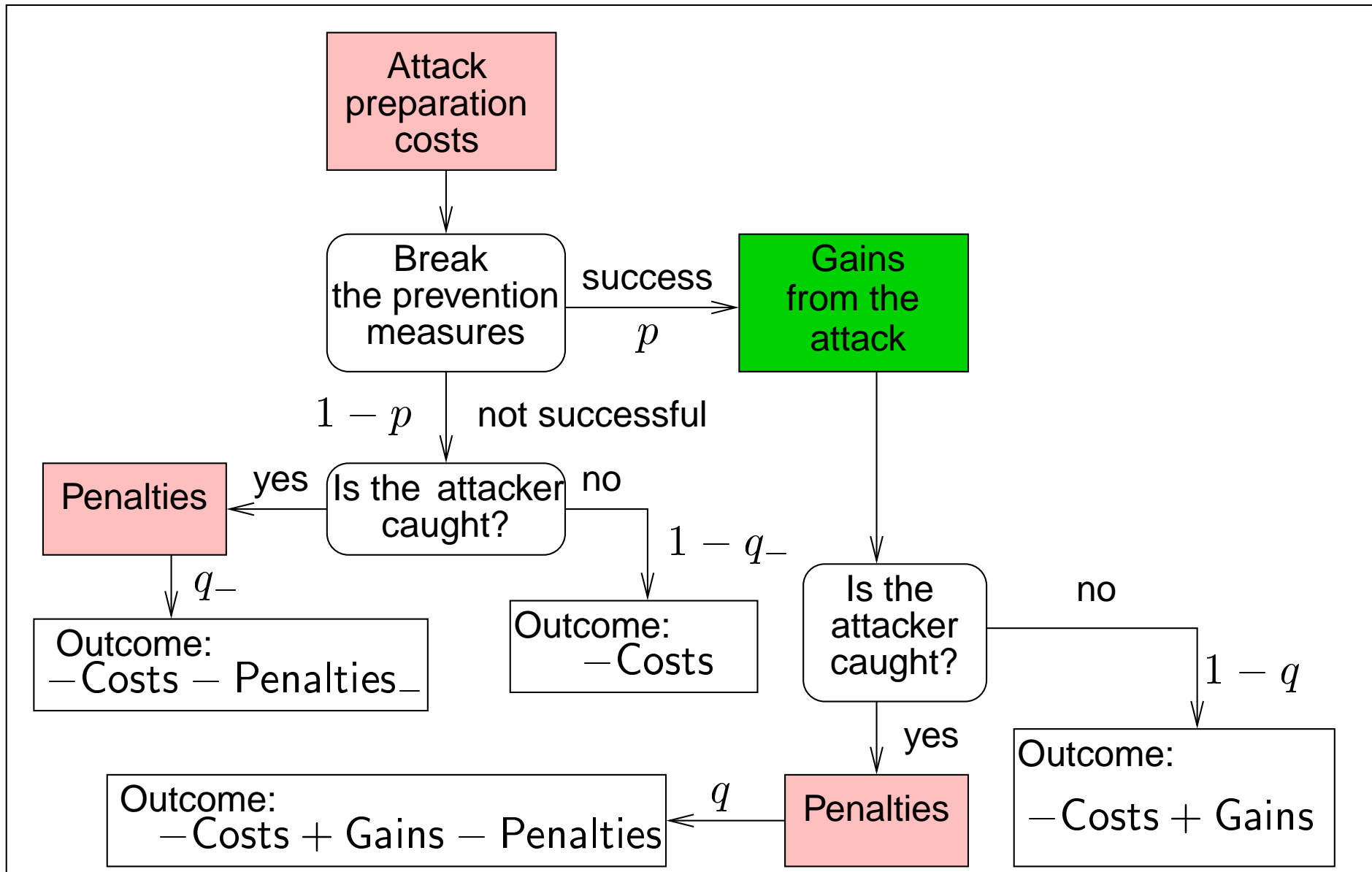
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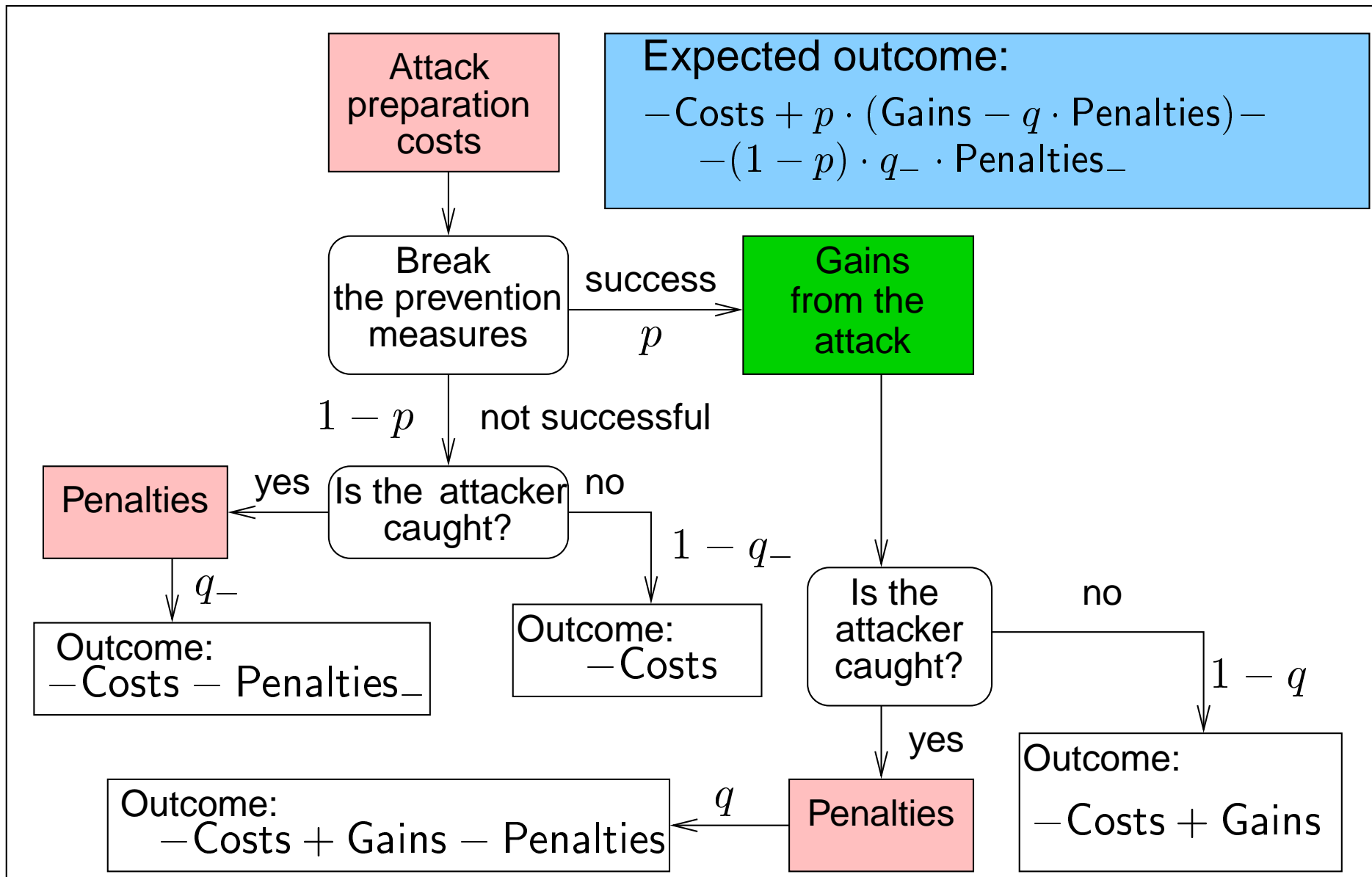
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# Tree Computations (I)

- Denoting  $\pi = q \cdot \text{Penalties}$  and  $\pi_- = q_- \cdot \text{Penalties}_-$ , we set the parameters  $(\text{Costs}, p, \pi, \pi_-)$  for every leaf node. Then we have

$$\text{Outcome} = -\text{Costs} + p \cdot \text{Gains} - p \cdot \pi - (1 - p) \cdot \pi_-$$

- For an OR-node with child nodes with parameters  $(\text{Costs}_1, p_1, \pi_1, \pi_{1-})$  and  $(\text{Costs}_2, p_2, \pi_2, \pi_{2-})$  the parameters  $(\text{Costs}, p, \pi, \pi_-)$  are computed as:

$$(\text{Costs}, p, \pi, \pi_-) =$$

$$\begin{cases} (\text{Costs}_1, p_1, \pi_1, \pi_{1-}), & \text{if } \text{Outcome}_1 > \text{Outcome}_2 \\ (\text{Costs}_2, p_2, \pi_2, \pi_{2-}), & \text{if } \text{Outcome}_1 \leq \text{Outcome}_2 \end{cases}$$

# Tree Computations (II)

- For a AND-node with child nodes with parameters  $(Costs_1, p_1, \pi_1, \pi_{1-})$  and  $(Costs_2, p_2, \pi_2, \pi_{2-})$  the parameters  $(Costs, p, \pi, \pi_-)$  are computed as follows:

$$Costs = Costs_1 + Costs_2$$

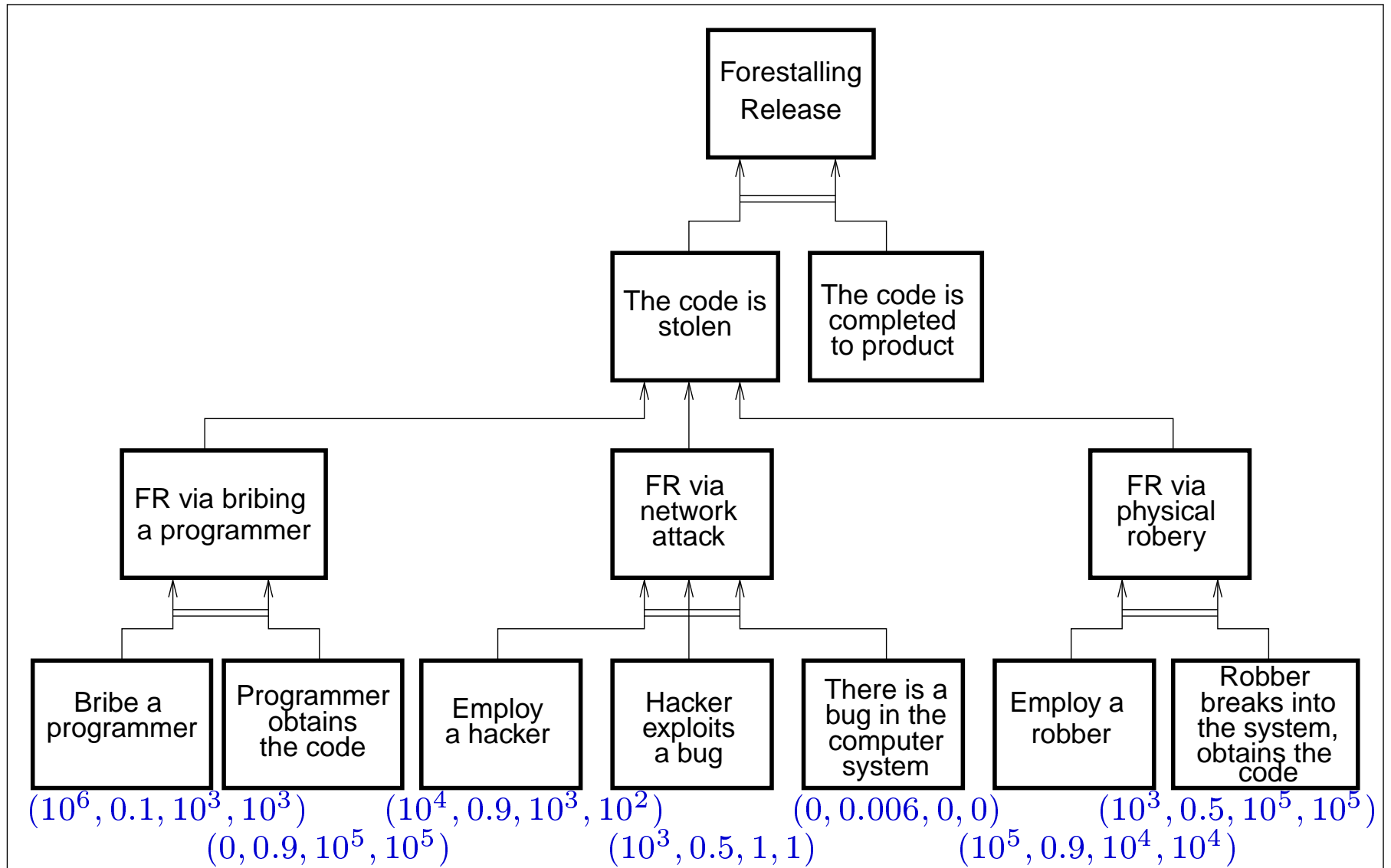
$$p = p_1 \cdot p_2$$

$$\pi = \pi_1 + \pi_2$$

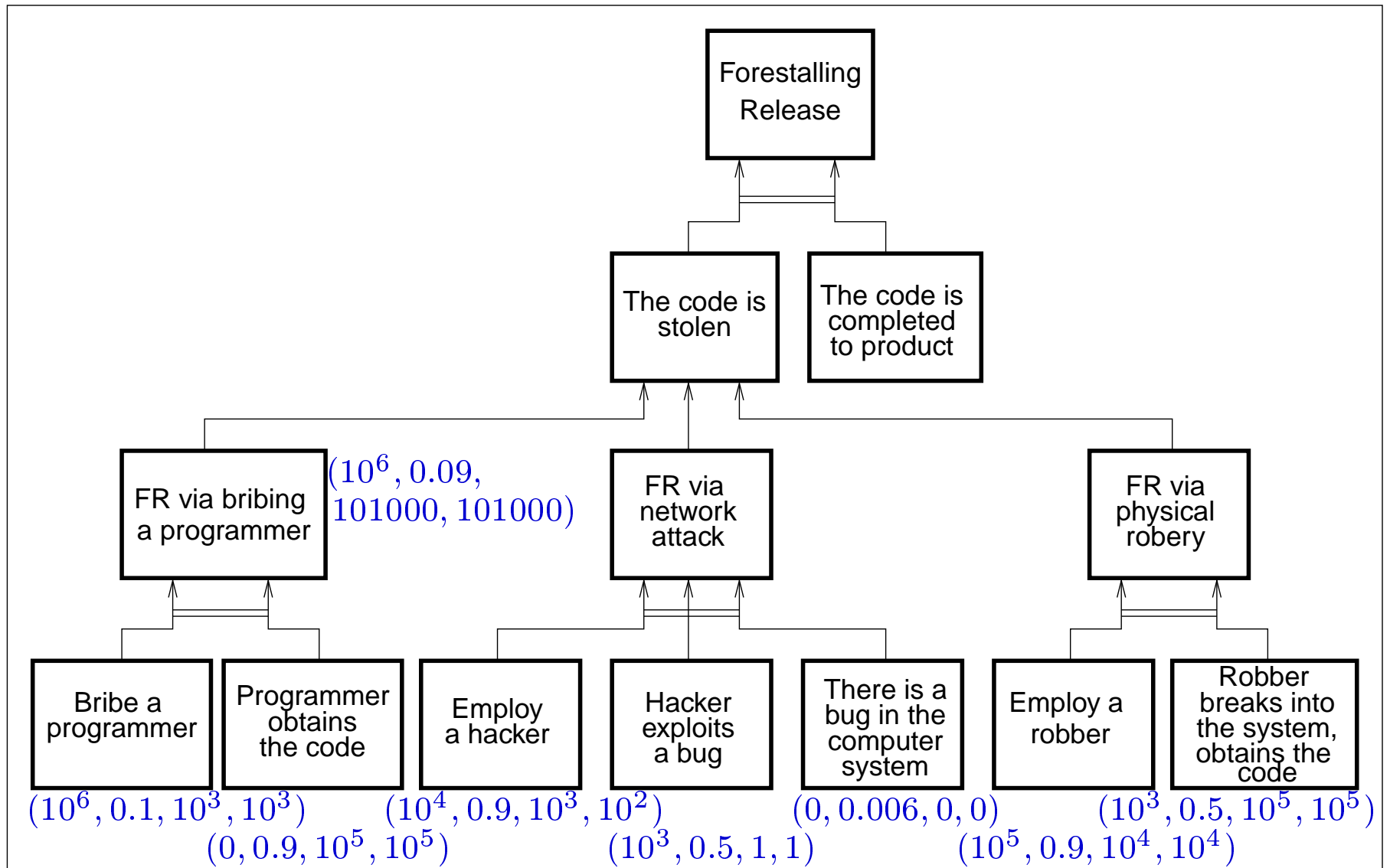
$$\pi_- = \frac{p_1(1 - p_2)(\pi_1 + \pi_{2-}) + (1 - p_1)p_2(\pi_{1-} + \pi_2)}{1 - p_1p_2} + \frac{(1 - p_1)(1 - p_2)(\pi_{1-} + \pi_{2-})}{1 - p_1p_2}$$

- The last formula represents the average penalty of an attacker, assuming that at least one of the two child-attacks was not successful

# Tree Computations: Example

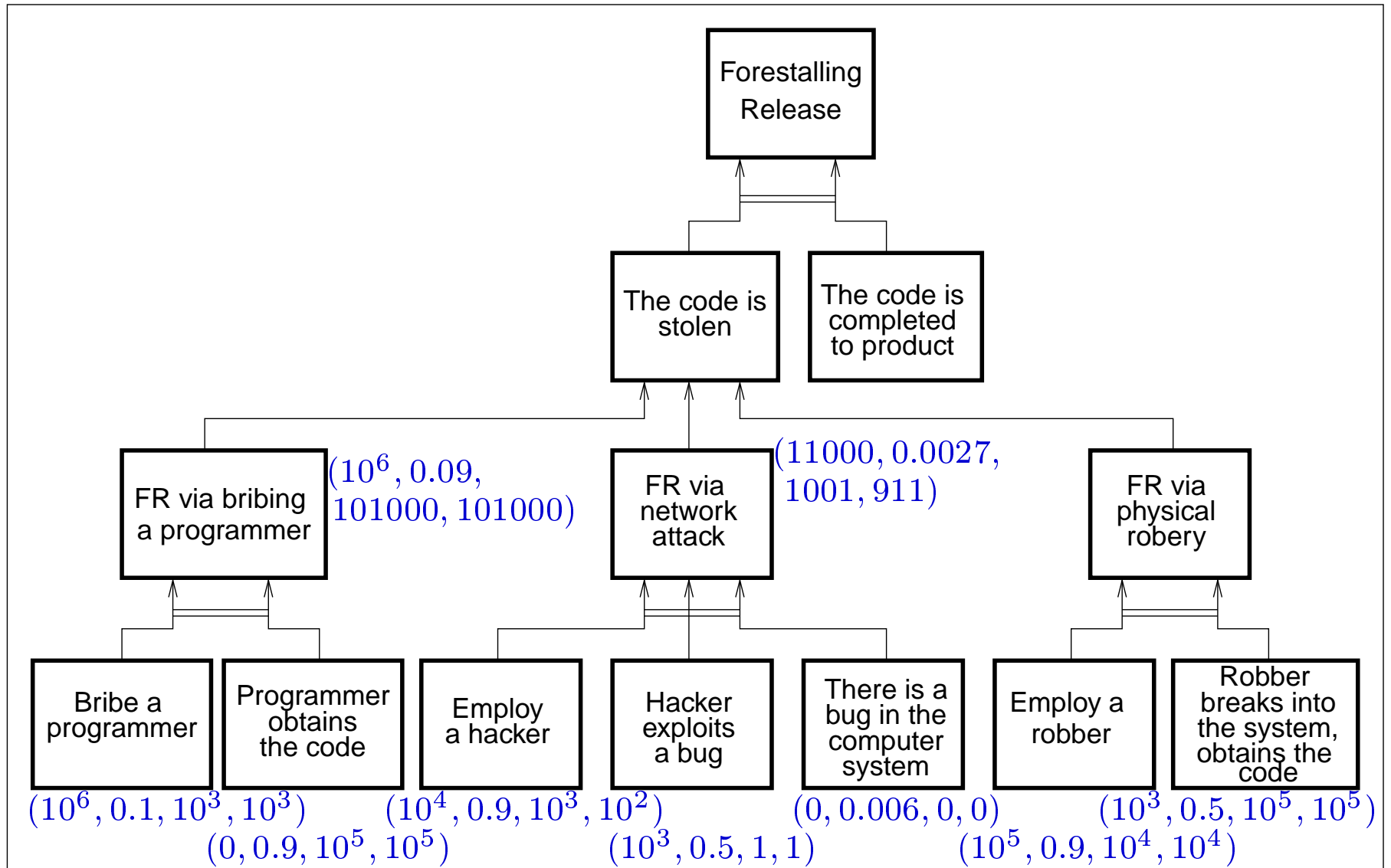


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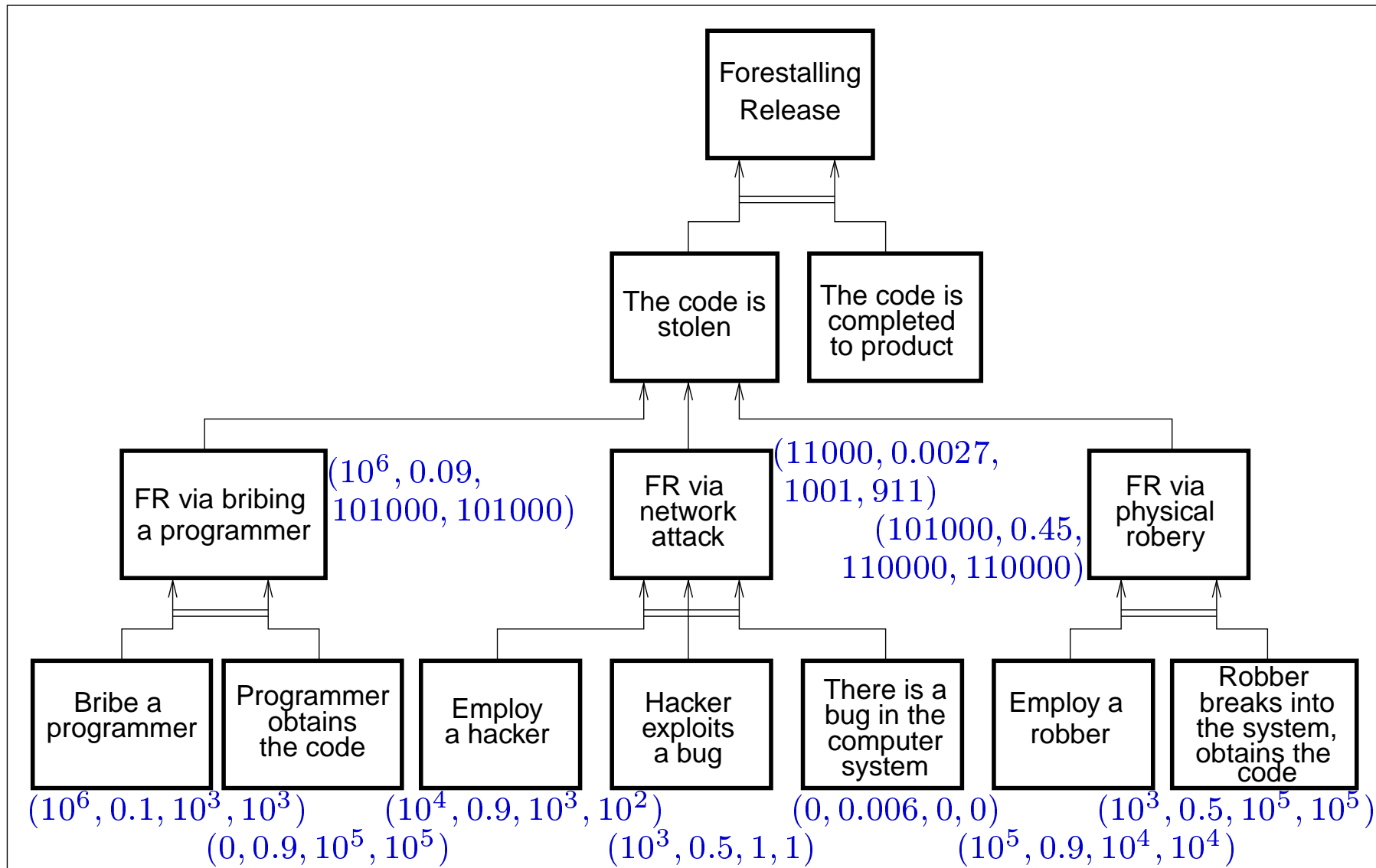




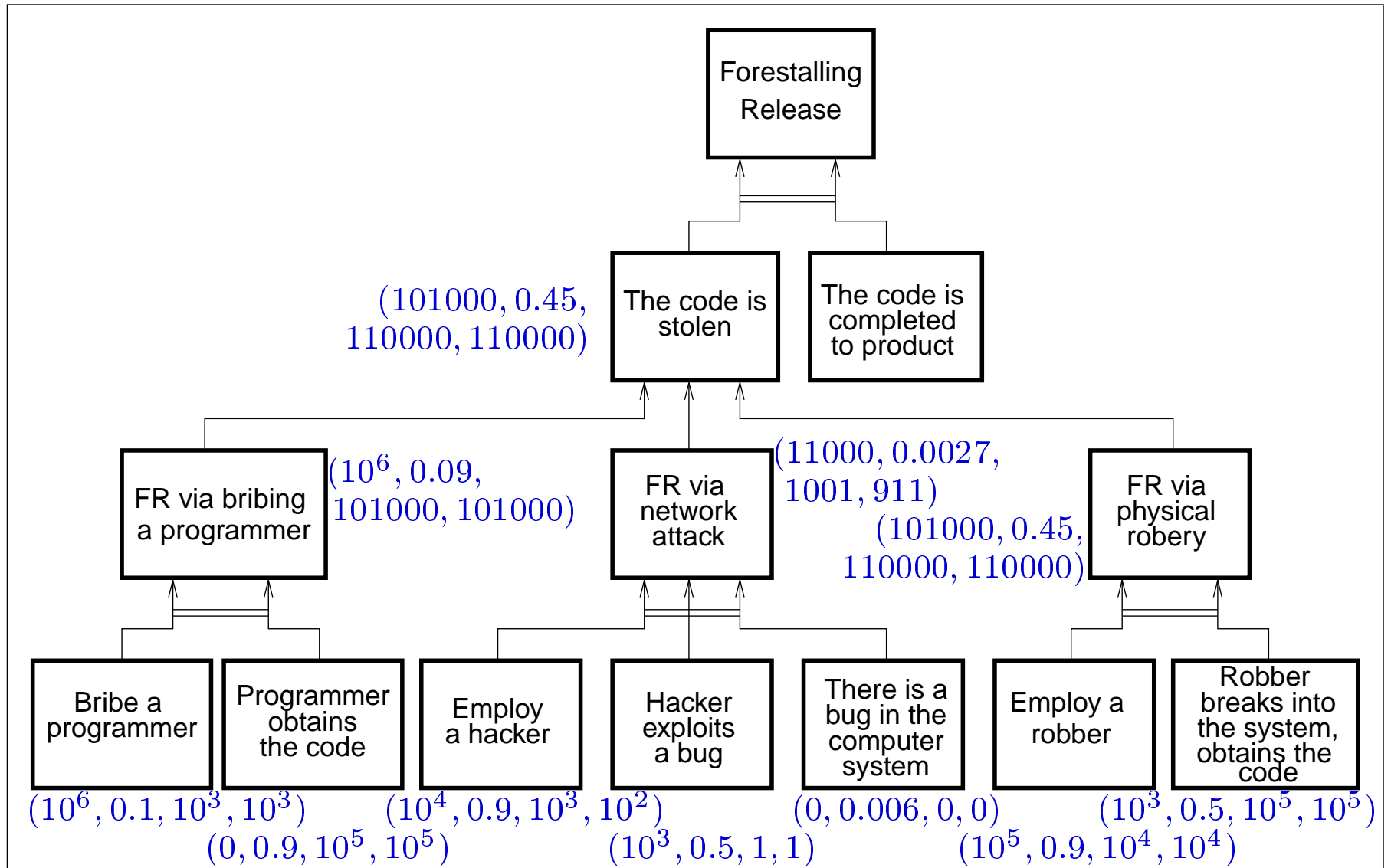
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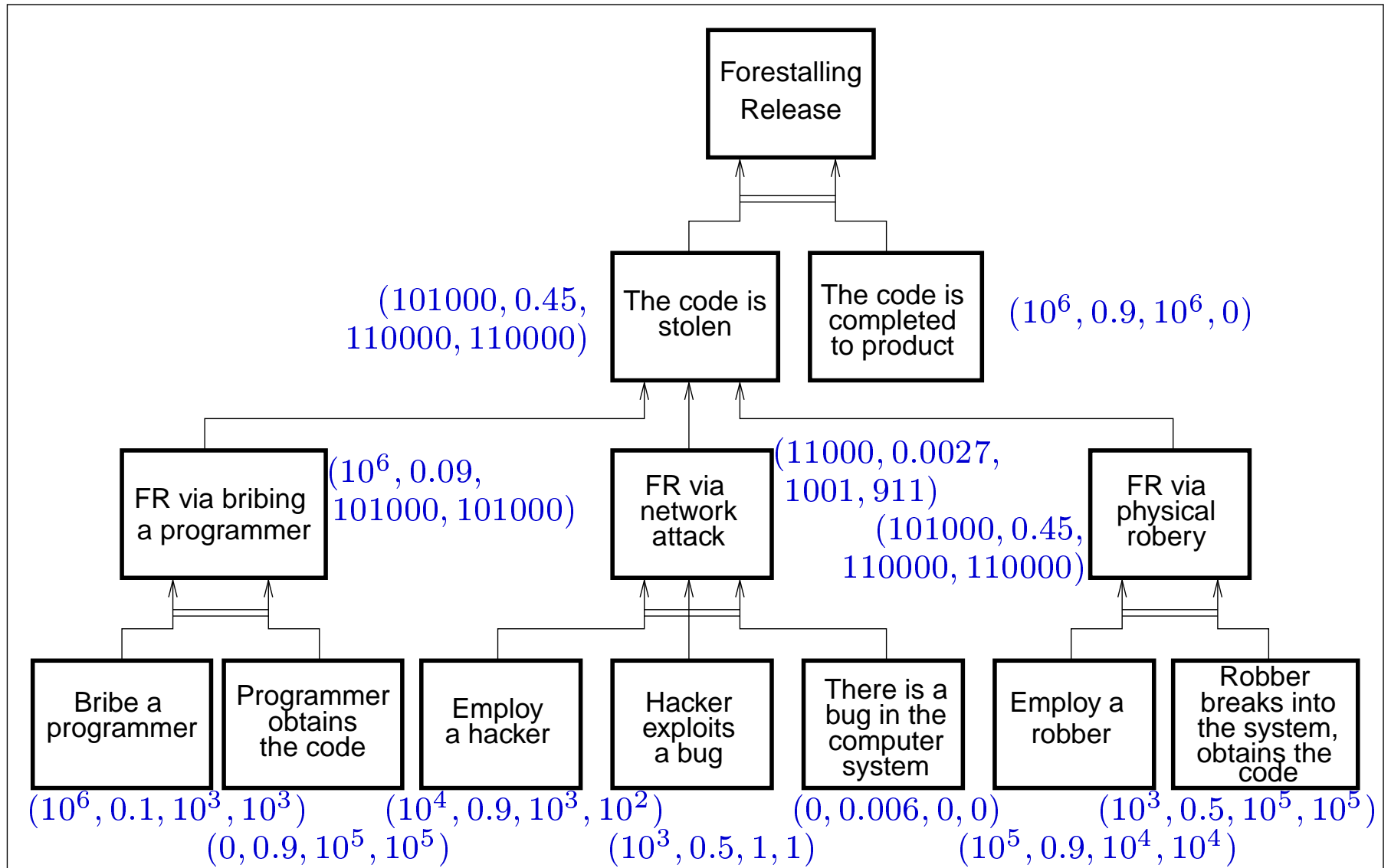
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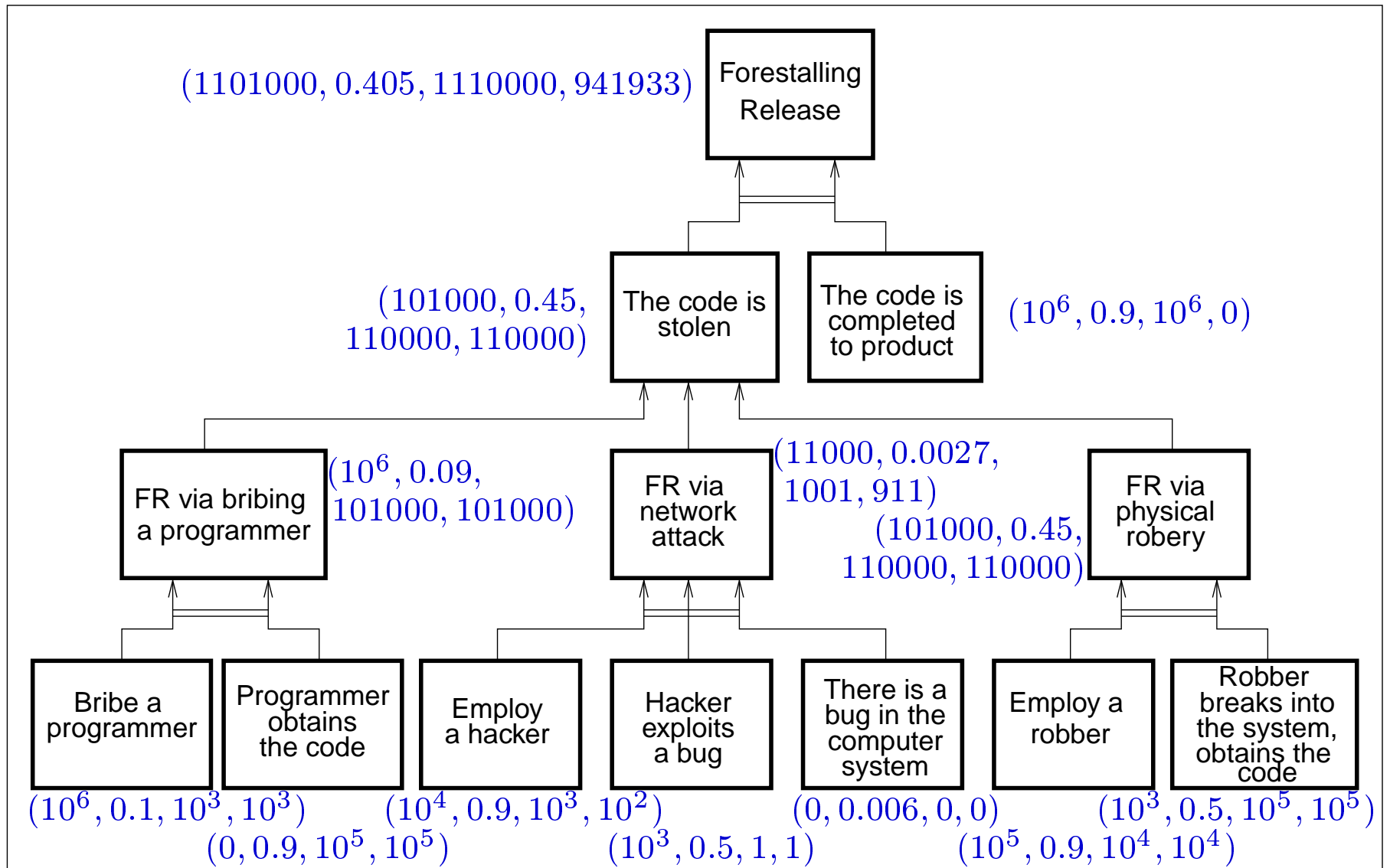
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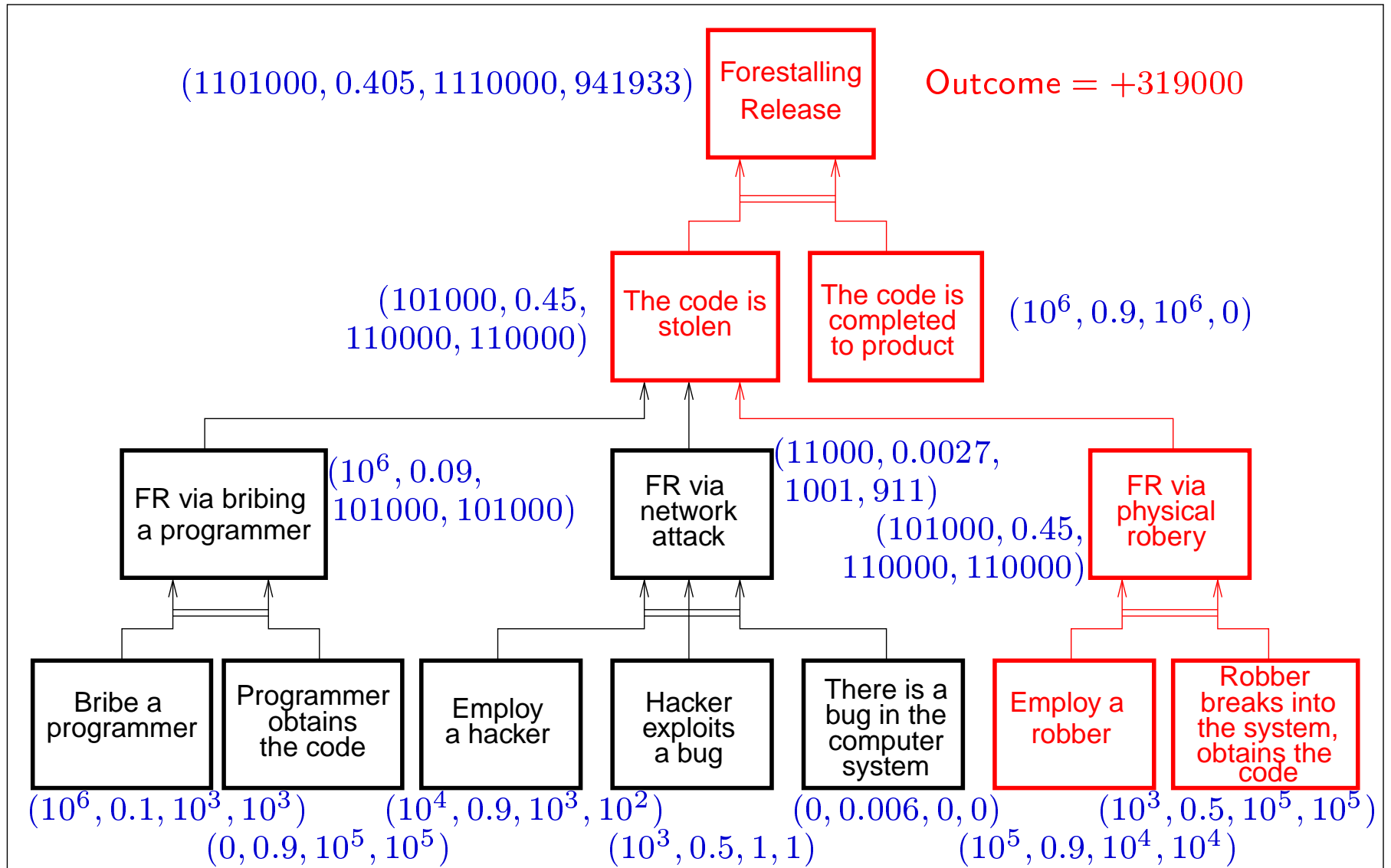
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# Evaluating Security Measures

- After building the attack tree, we can evaluate and compare potential security measures
- Security measures may
  - increase detection probability, hence increasing  $\pi$  and/or  $\pi_{-}$ ,
  - increase Costs of the attack,
  - reduce the probability  $p$  of the attack success.
  - etc
- We can then change the respective parameters, make the tree computations again and see, whether the Outcome has become negative

# Modeling Parameter Estimations

- Usually, when an expert evaluates some parameter, his estimation is not absolute, but holds with some confidence
- Thus, we can consider *estimated values* of the form

$$p_X = \Pr[k_1 \leq X \leq k_2] ,$$

where  $p_X$  is the *probability* of the unknown value of the parameter  $X$  being within the interval of  $[k_1, k_2]$



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- *How does one compute with estimated values?*

# Estimation Arithmetic – Operations

Our tree computations need the following arithmetic primitives:

- Adding a fixed real number
- Multiplying by a fixed real number
- Adding/subtracting two estimated values
- Multiplying two estimated values
- Dividing two estimated values
- Comparing two estimated values

# Estimation Arithmetic – Basic Pattern

The basic pattern of all the estimation arithmetic operations is the following:

- Convert the estimations to normally distributed random variables
  - If needed, centralize them to mean value 0
- Compute with the random variables
- Convert the resulting random variable back to an estimation
  - If needed, de-centralize

# Estimation $\rightarrow$ Random Variable

- To convert the estimation  $\mathcal{X}$  to a random variable  $X$ , we have to find out the mean  $a_X$  and standard deviation  $\sigma_X$ :

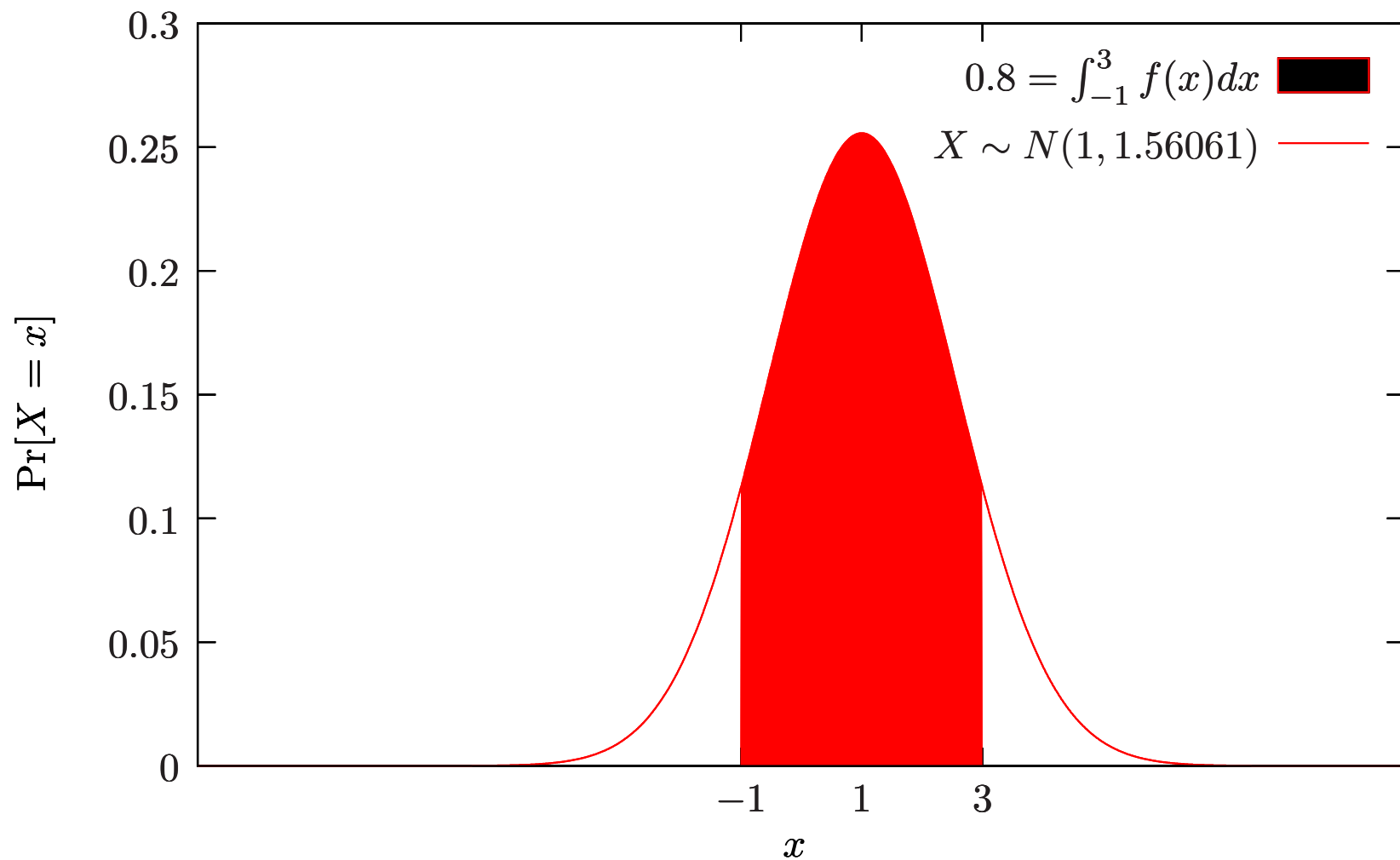
$$a_X = \mathbf{E}X = \frac{k_1 + k_2}{2} ,$$

$$p_X = \Pr(k_1 \leq X \leq k_2) = \Phi\left(\frac{k_2 - a_X}{\sigma_X}\right) - \Phi\left(\frac{k_1 - a_X}{\sigma_X}\right) ,$$

where the  $\Phi(x)$  is the Laplace's function

- We denote conversion of estimation  $\mathcal{X}$  to normally distributed random variable  $X$  as  
 $\mathcal{X} = (p_X, k_1, k_2) \rightarrow X \sim N(a_X, \sigma_X)$

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# Random Variable $\rightarrow$ Estimation

- To convert the probabilistic variable  $X$  back to an estimation  $\mathcal{X}$ , we need to specify the confidence  $p'_X$
- To simplify the operations with our estimations of the attack-tree node parameters, we will convert all estimations to the same global confidence level  $p_T$
- In effect,  $p_T$  defines the confidence level or the margin of error at which we would like to have the answer of our attack-tree analysis given
- If the original estimation  $\mathcal{X}$  of an expert is given using some other confidence level  $p_X$ , we first convert  $\mathcal{X} = (p_X, k_1, k_2) \rightarrow X \sim N(a_X, \sigma_X)$  and then find the new interval  $[k'_1, k'_2]$  by  $X \sim N(a_X, \sigma_X) \rightarrow \mathcal{X} = (p_T, k'_1, k'_2)$

# Soundness of Computations

- Most parameters of the nodes have a limited value domain, e.g.  $\text{Cost} \geq 0$  and  $p \in [0, 1]$
- However, as a result of conversions and tree computations, some values may drop out of this domain
- Generally, such a situation indicates that no sound conclusions can be drawn on the given confidence level  $p_T$ . This problem can be solved in a number of ways:
  - The global confidence level  $p_T$  can be decreased. It is possible to find the largest value  $p_T$  ensuring sound conclusions and this value can be considered as the confidence level of the whole tree
  - It is possible to define the required confidence level locally for each node



# Result Interpretation

- As a result of the computations, Outcome of the root node is found as an estimation  $\mathcal{X} = (p_X, k_1, k_2)$ . There are three possible major cases:
  - $0 < k_1 < k_2$  – the vulnerability level is *high*;
  - $k_1 < k_2 < 0$  – the vulnerability level is *low*;
  - $k_1 \leq 0 \leq k_2$  – the vulnerability level is *medium*
    - $\frac{k_1+k_2}{2} < 0$  – the vulnerability level is *lower medium*
    - $\frac{k_1+k_2}{2} > 0$  – the vulnerability level is *higher medium*

# Further directions

- More case studies
- An analysis tool
- Tree computations are known to be imprecise
  - We use Gains in every internal node, even though the attacker gets the whole gain after the primary threat has been materialized
  - Precise computations can not be done as tree computations – we would need to consider all the subsets of the leaf set
  - Can this work be optimized?

**Thank You!**

Questions?